

1 Complications for Computational Experiments from 2 Modern Processors*

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11 — Abstract —

12 In this paper, we revisit the approach to empirical experiments for combinatorial solvers. We provide
13 a brief survey on tools that can help to make empirical work easier. We illustrate origins of uncertainty
14 in modern hardware and show how strong the influence of certain aspects of modern hardware and
15 its experimental setup can be in an actual experimental evaluation. More specifically, there can be
16 situations where (i) two different researchers run a reasonable-looking experiment comparing the
17 same solvers and come to different conclusions and (ii) one researcher runs the same experiment
18 twice on the same hardware and reaches different conclusions based upon how the hardware is
19 configured and used. We investigate these situations from a hardware perspective. Furthermore, we
20 provide an overview on standard measures, detailed explanations on effects, potential errors, and
21 biased suggestions for useful tools. Alongside the tools, we discuss their feasibility as experiments
22 often run on clusters to which the experimentalist has only limited access. Our work sheds light on
23 a number of benchmarking-related issues which could be considered to be folklore or even myths.

24 **2012 ACM Subject Classification** Computer systems organization → Multicore architectures; Hard-
25 ware → Temperature monitoring; Hardware → Impact on the environment; Hardware → Platform
26 power issues; Theory of computation → Design and analysis of algorithms

27 **Keywords and phrases** Experimenting, Combinatorial Solving, Empirical Work

28 **Digital Object Identifier** 10.4230/LIPIcs.CP.2021.55

29 **Funding** Johannes K. Fichte: Google Fellowship at the Simons Institute, UC Berkeley.

30 Markus Hecher: FWF Grants Y698 and P32830 and Grant WWTF ICT19-065.

31 **Acknowledgements** Authors are given in alphabetical order. The work has been carried out while
32 the first three authors were visiting the Simons Institute for the Theory of Computing.

33 **1** Introduction

34 “Why trust science?” is the title of a recent popular science book by Naomi Oreskes [74]. We
35 can ask the same question of combinatorial sciences, algorithms, and evaluations: *Why trust*
36 *an empirical experiment?* Roughly speaking, in science, we try to understand why things
37 happen in the real world and investigate them with the help of scientific methods. One
38 important aspect to make an empirical evaluation trustworthy is reproducibility. This topic
39 has been the subject of much recent scrutiny, with some arguing there is a reproducibility
40 crisis in areas fields of computer science [33, 31] and even a replicability crisis in other scientific

* This work was done in part while the first three authors were participating in a program at the Simons Institute for the Theory of Computing.



41 fields of research [81]. Luckily in combinatorial problem solving, replicability is often already
 42 indirectly addressed in public challenges, which many combinatorial solving communities
 43 organize in order to foster implementations and evaluations [47, 82, 80, 83, 86, 20, 21]. The
 44 challenges provide a place for empirical evaluations, feature shared benchmarks, and support
 45 long-term heritage [3, 17, 22, 54]. It is therefore often assumed that everything should be
 46 judged with respect to these benchmarks or latest solvers [5]. However, benchmarks featured
 47 in competitions are not necessarily robust [40, 49] and might bias towards existing solving
 48 approaches and heuristics. On that account, one can argue that non-competitive evaluations
 49 are quite helpful for papers that are orthogonal to classical improvements over one particular
 50 solving technique or algorithm [19, 30]. There, one can often see a strong focus on algorithm
 51 engineering and their evaluation [63], which might not always be desired from a theoretical
 52 perspective. In particular, it makes reproducibility far less obvious than one would expect from
 53 theory. While reproducibility initiatives are becoming fashionable [73, 59], aspects are often
 54 left out in practical algorithm engineering and when testing combinatorial implementations:
 55 (i) the test-setup is not given (*no protocol*) or error prone (*no failure analysis/considerations*),
 56 (ii) modern hardware is simplified to the von-Neumann model (Princeton architecture) [87]
 57 and considered deterministic, and (iii) underlying software is neglected.

58 In this work, we summarize a list of topics to consider that might be folklore to an
 59 experienced engineer, but are often only mentioned between the lines while being crucial to
 60 actual reproducibility (Section 2.1). We include a list of *system and environment parameters*
 61 that are impactful when carrying out empirical work (Section 2.3). We summarize useful
 62 tools and list *practical problems* that repeatedly occur when experimenting (Sections 3.1,
 63 3.2, and 3.3). In the main part of our paper, we provide an initial *list of issues* caused by
 64 modern consumer hardware that can have a notable impact if setup and configurations are
 65 not carefully designed (Table 1). We show by example that *one can achieve different results*
 66 in the number of solved instances ranging from 5%–40% on the same hardware, depending
 67 on the setup (Experiment 1, Table 3). This could suggest that it is not always meaningful to
 68 only prefer solvers that beat the “best” solver, but to aim for *clean benchmark settings* and
 69 elaborate discussions that highlight both the solver’s advantages and disadvantages.

70 **Related Works.** There are various works that address aspects of reproducibility [3, 7,
 71 8, 15, 16, 56, 79, 94, 98] and experimental design [39, 63, 71], including micro-benchmarking,
 72 which requires special attention in terms of statistical analysis [42], [71, Ch.8]. Previous
 73 works neglected effects of modern parallel hardware on experimenting and some aspects have
 74 only been addressed in the background by the community. We put attention on certain issues
 75 arising on modern machines, updating outdated assumptions on measures, and illustrating
 76 how certain problems can be omitted. In the sequel, we revisit some of these related works.

77 **2 Evaluating Combinatorial Algorithms**

78 Natural sciences have a long tradition in designing experiments (DOE). Practical experiments
 79 date back to the ancient Greek philosophers such as Thales and Anaximenes with empirically
 80 verifiable ideas. There, *methodology is key* and has a long tradition with formal approaches
 81 existing since the late 1920s [25, 26]. Methodology not only involves the experiment itself,
 82 but also observation, measurement, and the design of test aiming to reduce external influence.
 83 Already in 1995, Hooker [39] discussed challenges in competitive evaluations of heuristics. A
 84 variety of these challenges are still of relevance in today’s combinatorial solving community.
 85 In particular, emphasis on competitions tells which algorithms/implementations are better,
 86 but not *why*; this remains a particularly big challenge in the SAT community [27, 91]. If
 87 a novel implementation wins, it is accepted; otherwise, it is considered as failure, resulting

88 in a high incentive to find the best possible parameter settings. The challenge of designing
89 an experiment (DOE) has meanwhile been addressed by a more experimental community
90 in broad guides [63] or algorithm engineering works [71]. In contrast, theoretical computer
91 scientists often neglect environmental considerations due to the assumption that modern
92 hardware behaves similar to simplified mathematical machine models [90] or classical hardware
93 models [93]. Unfortunately, this is no longer the case for modern architectures. There is a
94 list of concepts and external influences that can interfere, some of which are discussed below.

95 2.1 Repeatability, Replicability, and Reproducibility

96 When conducting a study or experiment, a central goal is to reduce inconsistencies between
97 theoretical descriptions and actual experiments. Three major principles play a central role:
98 repeatability, replicability, and reproducibility. Unsurprisingly, these topics are also critically
99 discussed in other scientific fields [65] and sometimes confused with each other.

100 *Repeatability* requires repeating a computation by the same researcher with the same
101 equipment at reliably the same result. The main purpose is often to estimate random
102 errors inherent in any observation. When evaluating combinatorial solvers, repeatability
103 translates to running the same solver with the same configuration on a given instance multiple
104 times, maybe even on different hardware. Some publicly accessible evaluation platforms
105 for combinatorial competitions address repeatability to a certain extent, as for example,
106 StarExec [84] and Optil.io [94]. Effective tools to measure and control the execution of
107 combinatorial solvers are runsolver [79] and BenchExec [7, 8].

108 *Replicability*, sometimes also called method reproducibility, refers to the principle that if
109 an experiment is replicated by independent researchers with access to the original artifacts
110 and same methodology, that then outcomes are the same with high confidence. When
111 evaluating combinatorial solvers, replicability translates to running the same solver with the
112 same configuration and instance on a different system by independent researchers, which is
113 sometimes also called *recomputability*. Relevant aspects relate to works such as the Heritage
114 projects [3, 16, 15], which preserve access to old solvers and making sources accessible
115 to a broad community, or Singularity, which aims for easy an setup on high-performance
116 computing (HPC) systems with few prerequisites on the environment [56, 98]. Another
117 initiative (Guix) aims for a dedicated Linux distribution that provides highly stable system
118 dependency configurations [1, 96]. Already in 2013, the recomputation manifesto postulated
119 that one can only build on previous work if it can properly be replicated as a first step [28].
120 In addition, it makes research more efficient, similarly to how high quality publications
121 can benefit other researchers. In contrast, some researchers argue that replicability is not
122 worth considering, since sharing all artifacts is a non-trivial activity, which in consequence
123 wastes efforts of the researchers [18]. Still, replicability is getting solid attention within the
124 experimental algorithmics community [73], since it supports quality assurance.

125 *Reproducibility* aims for being able to obtain the same outcome using artifacts, which
126 independent researchers develop without help of the original authors. When evaluating
127 combinatorial solvers reproducibility roughly refers to another group constructing a second
128 solver that implements the same algorithmic ideas. For example, Knuth re-implemented SAT
129 algorithms from several epochs [52]. More experimental directions are investigations into
130 robustness of benchmark sets and their evaluation measures [49]. Reproducibility can also
131 be interpreted fairly vaguely [32]. Interestingly, the literature on experimental setup [63] and
132 algorithm engineering [71] already contains a variety of suggestions to obtain reproducibility.

133 Repeatability and to some extent also replicability are the focus of our paper. Our aim
134 is to make researchers aware of potential problems caused by modern computer systems,

135 illustrate how to detect and reduce them without spending hours of debugging or over-
 136 valuing small improvements. Before we go into details, we briefly discuss principles and
 137 tools that support both repeatability and replicability. Since recent works on reproducibility
 138 provide various helpful suggestions on replicability in terms of environment [75], we focus
 139 only on aspects that might degrade long-term repeatability and replicability, resulting in
 140 over-engineering or over-tooling. We argue in favour of reviving an old Unix philosophy:
 141 build simple, short, clear, modular, and extensible code [64] both for the actual solver as
 142 well as the evaluation. Always keep dependencies low and provide a statically linked binary
 143 along with your code [89, 60] or a simple virtual environment to reproduce dependencies if
 144 you use interpreted languages. Even if the source code does not compile with newer versions,
 145 binary compatibility is mostly maintained for decades. The primary focus of container-based
 146 solutions, such as Singularity [56], is current accessibility of scientific computing software
 147 that requires extensive libraries and complex environments. It is quite useful if the software
 148 is widely used, requires complicated setup on high performance computing environments, and
 149 is continuously maintained. Container-based solutions can also be useful for building source
 150 code on old operating systems [3]. However, they introduce additional dependencies, increase
 151 conceptual complexity, can have notable runtime overhead under certain conditions [100],
 152 require additional work for a proper setup (both hosts as well as containers), and increase
 153 chances that the software does not out run of the box in 3 years. A practical observation
 154 illustrates this quite well: already since 2010, a meta software (Vagrant) tries to wrap
 155 providers such as VirtualBox, Hyper-V, Docker, VMWare, or AWS. While virtualization can
 156 be tempting to use, chances are high that some of these providers upgrade functionality or
 157 disappear entirely resulting in useless migration efforts.

158 2.2 An Experiment

159 In the beginning of Section 2, we stated classical experimental viewpoints: fixed solver or
 160 fixed instance set. In contrast, we take a third perspective by fixing both the instance
 161 set and the solver and focus on differences in hardware configurations. Therefore, we turn
 162 our attention to a recent experiment on SAT solvers (time leap challenge) [22]. We repeat
 163 the experiment with the solver `CaDiCa1` on other hardware to investigate side effects of
 164 experimental setup and hardware. Also, we use *set-asp-gauss* as instances, which contains
 165 200 publicly available SAT instances from a variety of domains with increasing practical
 166 hardness [40]¹. We take a timeout of 900 seconds, but would like to point out that recent
 167 SAT competitions restrict the total runtime over all instances to 5,000 seconds. We run
 168 experiments on the following environments: COMET LAKE (I7 GEN10): Intel i7-10710U
 169 4.7 GHz, Linux 5.4.0-72-generic, Ubuntu 20.04; HASWELL (XEON GEN4): 2x Intel Xeon
 170 E5-2680v3 CPUs, Linux 3.10.0-1062, RHEL 7.7; ROME (ZEN2): 2x AMD EPYC 7702,
 171 Linux 3.10.0-1062, RHEL 7.7; and SKYLAKE (XEON GEN6): Xeon Silver 4112 CPU, Linux
 172 version 4.15.0-91, Mint 19. We explicitly include cheap mobile hardware by using a COMET
 173 LAKE (I7 GEN10) CPU, since not every group can afford expensive server hardware or spend
 174 valuable research time on setting up stable experiments on a cluster.

175 Table 1 illustrates the results of the experiment on varying hardware. Unsurprisingly, the
 176 modern hardware running at 4.7 GHz solves the most instances. Somewhat unexpected is
 177 that two potentially faster processors solve fewer instances. Namely, the Rome CPU which

¹ The benchmark set is available for download at <https://www.cs.uni-potsdam.de/wv/projects/sets/set-industrial-09-12-gauss.tar.xz>

Processor (CPU)	f	p	$s(15)$	$t[h]$
SKYLAKE	3.0	1	190	5.12
HASWELL	3.3	1	189	3.89
ROME	3.4	1	190	3.79
COMET LAKE	4.7	1	191	3.81
COMET LAKE	4.7	6	189	6.13
COMET LAKE	4.7	12	176	7.18

■ **Table 1** Number of solved instances out of 200 SAT instances running the solver CaDiCa1 on varying platforms. Column $s(15)$ contains the number of solved instances when timeout is 15 minutes; f and p refer to the CPU frequency in GHz and number of solvers running in parallel, respectively. The t column contains the total runtime in hours for all instances solved within 15 minutes.

178 is faster than the Skylake CPU solves fewer instances and similarly the Haswell solves fewer
 179 instances than the Skylake. Since both processors are different generations one might expect
 180 that the AMD CPU is simply slower. While the 5% fewer solved instances might seem not
 181 much comparing the results to the ones of the time leap challenge, it would mean that a
 182 ten year old solver solves almost the same number of instances on a modern hardware as
 183 CaDiCa1 on very recent hardware. Below, we explain that this is clearly not the case and
 184 illustrate details of the experimental setup that contribute to the low number of solved
 185 instances. In contrast, when comparing the number of solved instances for the COMET LAKE
 186 configurations, it is obvious to an experienced reader that while the COMET LAKE CPU
 187 exposes 12 software cores, due to multithreading (MT) only 6 physical cores are available.
 188 Still, when using all physical cores, we have more than 30% higher runtime, which can be
 189 particularly problematic when comparing to settings that prefer total runtime as measure. To
 190 avoid this, we could simply not run solvers in parallel; however, this seems quite impractical
 191 and inefficient. In the following sections, we clear up which problems in the setup may have
 192 caused the differences and illustrate how to avoid such issues.

193 2.3 Uncertainty on Modern Hardware

194 Modern processors can do many calculations at the same time by using multiple cores on each
 195 processor and each core also has built-in a certain parallelism. While this can be exploited
 196 explicitly in terms of parallel programming frameworks, some features are already done by
 197 on-board circuits or firmware, which is a low level software layer between the CPU hardware
 198 and the operating system. Compile time optimizations such as *automated parallel execution*
 199 *optimization* and *cache performance optimization* [4] can then automatically employ specific
 200 features. For example, *loop optimization* tries to automatically rewrite loops in programs such
 201 that the loop can be executed in parallel on multiprocessor systems. Scheduling splits loops
 202 so that they can run concurrently on multiple processors. Vectorization optimizes for running
 203 many loop iterations on parallel hardware that supports single instruction multiple data
 204 (SIMD). Therefore, instead of processing a single element of a vector N times, m elements
 205 of a vector are processed simultaneously N/m times. In fact, modern CPUs have so-called
 206 *vector instruction sets* such as SSE, AVX, NEON, or SVE depending on the architecture,
 207 which makes them SIMD hardware. Loop vectorization can have a significant impact on
 208 the runtime due to effects on pipeline synchronization or data-movement timing. Usually,
 209 dependency analysis tries to optimize these operations. But depending on the compiler
 210 (GCC, Intel, or LLVM) different runtimes of the resulting binary can be observed [92].

211 Processor specific features add to less pre-calculable behavior. *Turbo Boost*, which was
 212 introduced around 2008, allows to dynamically overclock the CPU if the operating system

213 requests the highest performance state of the processor [66]. *Thermal design power (TDP)*,
214 which was established around 2012, allows to scale the power (energy transfer rate) variably
215 between 50W and 155W [70] to save energy depending on the system load. In particular, this
216 is active on laptop systems that are not connected to an electrical outlet or if certain system
217 sensors detect high temperature. *Turbo Boost 2.0* was introduced around 2011 and it uses
218 time windows with different levels of power limits, so that a processor can boost its frequency
219 beyond its thermal design power, which can thus only be maintained for a few seconds without
220 destroying the CPU [2]. *Huge Pages*, which were increased to 1GB, can reduce the overhead
221 of virtual memory translations by using larger virtual memory page sizes which increases the
222 effective size of caches in the memory pipeline [24]. *Branch prediction*, whose early forms
223 already date back to the 1980s in SPARC or MIPS [68], speculates on the condition that
224 most likely occurs if a conditional operation is run. Modern CPUs have a quite sophisticated
225 branch prediction system, which executes potential operations in parallel [48]. The CPU
226 can then complete an operation ahead of time if it made a good guess and significantly
227 speed up the computation. This often depends on how frequently the same operation is used.
228 Otherwise, if the branch predictor guessed wrong, the CPU executes the other branch of
229 operation with some delay, which can be longer than expected as modern processors tend to
230 have quite long pipelines so that the misprediction delay is between 10 and 20 clock cycles.
231 The situation gets more complicated when substantial architectural bugs are mitigated or
232 patched, as this can notably slow down the total system performance [58, 53].

233 Clearly, we need practical empirical evaluations of algorithms and techniques and often-
234 times it is not useful to just restrict an evaluation to existing benchmarks used in competitions,
235 if they even exists. But just the “complications” or, more formally, source for an error in mea-
236 surement mentioned above, could make the outcome of an experiment far less deterministic
237 than one would expect. For that reason, we suggest a more rigorous process when evaluating
238 implementations, including the understanding of measurements and effects of potential errors
239 on the outcome as well as approaches to reduce unexpected and not entirely deterministic
240 effects. In a way, the following sections provide a modern perspective on simple measures
241 (runtime) that incorporate state-of-the-art in hardware and operating system technology.

242 **3 Measurements and Hardware Effects**

243 In the following, we discuss measurements used when evaluating runtime of empirical work.
244 Along with the measures, we recap useful measuring and controlling tools. Since most of the
245 tools are highly specific to the kernel in the used operating system, we restrict ourselves to
246 recent versions of Linux and widely used distributions thereof.

247 **3.1 Runtime**

248 When evaluating algorithms, a central question is how long its implementation actually runs
249 on the input data (runtime). There are five main measures that are interesting in this context:
250 real-time, user-time, system-time, CPU-usage, and system load. The *real-time*, frequently
251 just called *wallclock time*, measures the elapsed time between start and end of a considered
252 program (method entry and exit). In contrast, *CPU-time* measures the actual amount of
253 time for which a CPU was used when executing a program. More precisely, the *user-time*
254 measures how much CPU-time was utilized and *system-time* how much the operating system
255 has used the CPU-time due to system calls by the considered program. Both measures
256 neglect waiting times for input/output (I/O) operations or entering a low-power mode due
257 to energy saving or thermal reasons. There are more detailed time measures on time spent in

258 user/kernel space, idle, waiting for disk, handling interrupts, or waiting for external resources
259 if the system runs on a hypervisor. *CPU-usage* considers the ratio of CPU-time to the
260 CPU capacity as a percentage. It allows for estimating how busy a system is, to quantify
261 how processors are shared between other programs. The *system load* indicates how many
262 programs have been waiting for resources, e.g., a value of 0.05 means that 0.05 processes
263 were waiting for resources. The system load is often given as *load average* which states the
264 last average of a fixed period of time; by default, system tools report three time periods (1, 5,
265 and 15 minutes). If the load average goes above the number of physical CPUs on the system,
266 a program has to idle and wait for free resources on the CPU.

267 **Suggested Measure for Runtime.** When measuring runtime, the obvious measure is
268 to use elapsed time, so as to measure the real-time of a program. However, when setting
269 an experiment, we aim to (i) reduce external influences, (ii) conduct reasonable failure
270 analysis, or (iii) use an alternative measure in the worst-case. Real-time can be unreliable
271 on sequential systems as a program can be influenced by other programs running on the
272 system and the program competes on resources with the operating system. For that reason,
273 dated guides on experimenting suggested to run a clean system and obtain a magic overhead
274 factor, which follows Direction (ii) replacing an expected failure analysis. More recent guides,
275 follow Direction (iii) and suggest to use CPU-time [63, 71], mainly arguing that real-time
276 minus unwanted external interruption should roughly equal used CPU-time when evaluating
277 sequential combinatorial solvers that use a CPU close to 100%. However, we believe that the
278 best approach for an experimental setup is always to follow Direction (i) and reduce external
279 influences. Suggestions on CPU-time are outdated as modern hardware is inherently parallel.
280 Even small single-board computers such as the Raspberry Pi have multi-core processors.
281 This allows to run programs and the operating system simply in parallel. Still, CPU-time
282 might prove useful to estimate a degree of parallelism or debug unexpected behavior.

283 **Expected Errors.** Real-time is measured by an internal clock of the computer. Nowa-
284 days, hardware clocks are still not very accurate. Expected time drifts are about one second
285 per day [95], which is often negligible for standard experiments as micro-benchmarking is
286 anyways rarely meaningful. But, time drift can be far higher, for example, when system load
287 is very high [72] and systems run within virtual machine guests [44, 6, 85]. Since modern
288 cryptography still requires exact system times, all state-of-the-art operating systems synchro-
289 nize the system clock frequently. Unfortunately, many widely used tools do not incorporate
290 time drifts and corrections by time synchronization utilities. Thus, if time drifts are high
291 (virtual machines) or a misconfiguration of the synchronization service occurs, measures
292 can be completely unreliable. Note that we can expect difference between CPU-time and
293 real-time in cases where heavy or slow access to storage occurs, slow network is involved, or
294 unexpected parallel execution happens. However, this should be ground to investigate details
295 and either eliminate problems in the experimental setup or update problematic program
296 parts, if possible. A classical example occurs when using the ILP solver CPLEX, which sets by
297 default a number of threads equal to the number of cores or 32 threads (whichever number
298 is smaller). An issue, which can especially happen when measuring CPU-time, is due to the
299 operating system and specific tooling. Namely, a program starts multiple processes, e.g., the
300 program calls a SAT solver, but the monitoring tool captures only one process.

301 **Tools to Measure Runtime.** A standard system tool is `GNU time` [50], which provides
302 CPU-time, real-time, and CPU usage of an executed program when run with the command-
303 line flag `-v`. Note that `time` refers to a function in the Linux shell whereas `GNU time` can be
304 found at `/usr/bin/time`. `GNU time` suffers from issues with time skew. A compact, free, and
305 open source tool with extended functionality is `runsolver` [79]. It can be easily compiled

and requires only few additional packages, but also suffers from issues with time skew. An extensive monitoring tool is `perf`, which is available in the linux kernel since version 2.6.31 (2009) [101]. `Perf` provides statistical profiling of the entire system when run with flag `stat`. It is easy to use and well documented, but requires installation of an additional package, an additional kernel module, and setting kernel security parameters (`perf_event Paranoid`, `nmi_watchdog`) [55, 61]. However, `perf` is usually available on maintained HPC environments.

Restricting Runtime. Oftentimes when running experiments, we are interested in setting an upper bound on the runtime, let the program run until this time, then terminate and measure how many inputs have been solved successfully. Classical tools to impose a timeout are `timeout` [11], `prlimit` [13], and `ulimit` (obsolete [88]). These tools use a kernel function (`timer_create`) to register a timer. The tools notify the considered program about the occurred timeout by sending a signal to terminate the program, but only to the started program that is responsible to handle potentially started children (entire process hierarchy). For that reason, these tools are often useless or require to build additional wrapper scripts when running academic code, which often omit proper signal handling. A popular tool in the research community that circumvents these problems is the already above mentioned tool `Runsolver` [79], which uses a sampling based approach. It monitors and terminates the entire hierarchy of processes started by the tested program. However, signals are sent to child processes first, which may need additional exception handling in the tested program. Furthermore, the sampling-based approach may cause measurable overhead in used resources. `runexec` is modern and thorough tool for imposing detailed runtime restrictions. It can be found within the larger framework for reliable benchmarking and resource measurement (`BenchExec`) [14]. `runexec` uses kernel control groups (cgroups) to limit resources [46, 36]. Cgroups are precise, but cause a certain overhead and are fairly quite hard to use manually. Unfortunately, `BenchExec` does not directly support commonly used schedulers in HPC environments (except AWS), requires administrative privileges during setup, specially configured privileges at runtime, and fairly new distributions and kernels. It is only widely available on Ubuntu or systems running kernels of version at least 5.11.

Suggested Tooling. In principle, we find `runexec` quite helpful when restricting runtime. It is reliable and has very helpful features such as warning the user about unexpected high system loads. However, it has strong requirements, both in terms of privileges and dependencies, and can be hard to setup, especially in combination with existing cluster scheduling systems. `GNU time` and `timeout` are both system tools available out of the box. Though, when using `timeout` we require additional tools (e.g., `pstree`) and a bit of scripting to handle an entire process hierarchy. Still, both tools might be the best choice if only standard system resources are available and no libraries can be installed. For older systems that are well-maintained or where additional libraries can be installed, we suggest `runsolver` (enforcement) in combination with `perf` (measurement). Both tools keep setup and handling at a minimum. Issues on potential time-skew and sampling-based issues are minimized and more detailed statistics (memory) can be outputted if needed. However, using this tooling requires to check carefully if the system is over-committed or if `runsolver` terminated a program too late. If required kernel modules or security parameters for `perf` cannot be installed/set, `runsolver` in combination with `GNU time` can be a reasonable alternative.

3.2 CPUs and Scaling

Modern hardware has features to dynamically overclock the CPU, which then can run at high frequency for a short period of time (*Turbo Boost*). Frequency scaling can save energy (*Thermal power design*) when processes do not require full capabilities of the system. These

Processor	f_a	f_e	p	$s(15)$	$t[h]$	Processor	f_a	f_e	p	$s(15)$	$t[h]$
COPPERMINE	0.5	0.5	1	98	8.93	HASWELL	3.3	*2.5	1	189	3.89
COMET LAKE	4.7	0.5	1	160	9.99	SKYLAKE	3.0	†3.0	1	190	5.12
COMET LAKE	4.7	*0.8	1	174	9.09	COMET LAKE	4.7	3.9	1	191	3.81
COMET LAKE	4.7	1.5	1	177	7.12	ROME	3.4	2.0	1	190	3.79
COMET LAKE	4.7	2.0	1	189	5.13						

■ **Table 2** Number of solved SAT instances running the solver `CaDiCa1` on varying platforms. Column $s(x)$ contains the solved instances when the runtime is cut off after x minutes. f_a , f_e , and p refer to the available and effective frequency of the CPU in GHz and number of solvers running in parallel, respectively. The $t[h]$ column contains the total runtime in hours for all instances solved within 15 minutes. We enforced limits using kernel governor parameters. Frequencies marked by $*$ are CPU base-frequencies. $†$ we could not enforce frequencies due to administrative restrictions. For COPPERMINE (PIII), we directly list the results by Fichte et al. [22].

353 features can significantly impact performance and uncertainty on modern hardware [34].
 354 We provide a brief experiment in Section 3.3 to illustrate effects. Within the operating
 355 system, the concept is known as dynamic CPU frequency scaling or CPU throttling, which
 356 allows a processor to run at frequency that is not its maximum frequency to conserve power
 357 or to save the CPU from overheating if the frequency is beyond its thermally safe base
 358 frequency. In fact, modern operating systems have options to manually set performance
 359 states. In Linux, the CPU frequency scaling (CPUFreq) subsystem is responsible for scaling.
 360 It consists of three layers, namely, the core, scaling governors, and scaling drivers [97].
 361 Available capabilities to modify the CPU frequency depend on the available hardware and
 362 driver [97]. A *scaling governor* implements a scaling algorithm to estimate the required CPU
 363 capacity [12]. However, minimum and maximum frequency can also be fixed by modifying
 364 kernel values. Specifications of modern CPUs detail the safe operating temperature (*Thermal*
 365 *Velocity Boost Temperature*) that still allows to boost the cores to their maximum frequency.

366 **Tools to Modify the CPU Frequency.** The tool `cpupower` provides functions to
 367 gather information about the physical CPU and set the scaling frequency. The flag `frequency-`
 368 `info` lists supported limits, activated governor, and current frequency. The tool `turbostat`
 369 allows to obtain extended information about base frequency, the maximum frequency, and
 370 the maximum turbo frequency depending on how many cores are active. The program
 371 `frequency-set` allows to set the maximum and minimum scaling frequency using flags `-u`
 372 and `-d`, respectively. However, the values can also be manually read/set in the kernel by
 373 modifying a text file. The turbo needs to be manually modified depending on the driver [97].
 374 The current frequency can be tested explicitly by running the command: `perf stat -e`
 375 `cycles -I 1000 cat /dev/urandom > /dev/null`.

376 **Revisiting the Experiment.** With the knowledge of frequency scaling at hand, we
 377 focus our attention to Table 2. There, we state runtime results and number of solved
 378 instances in dependence of platform and CPU frequency. More precisely, the maximum CPU
 379 frequency and the chosen frequency scaling. Obviously, the runtime and number of solved
 380 instances significantly depends on the frequency scaling of the CPU, which already explains
 381 why CPUs that permit a higher frequency show less solved instances. From the number of
 382 solved instances for COMET LAKE (i7 GEN10) CPU and COPPERMINE (PIII) CPU, we can
 383 also see that an increase in CPU frequency alone is clearly not the reason for modern solvers
 384 running faster on modern hardware than on old hardware.

385 **Suggested Setup.** When handling thermal management for experiments, one usually
 386 balances between three objectives (i) stability and repeatability of the experiment; (ii) max-

387 inum speed vs (iib) throughput; and (iii) low effort or no access to thermal management
 388 functions of the operating system while aiming to balance (i) and (ii). If we focus our setup
 389 on Objective (i), a conservative choice is to set the CPU frequency to its base frequency
 390 and limit the parallel processes according to available NUMA regions. Then, the thermal
 391 management has limited effects on an experiment. Running the same experiment another
 392 system, where the CPU frequency was fixed to the same value and where the memory layout
 393 is comparable, shows similar results for CPU-intensive solvers. Such an approach could
 394 simplify certain aspects of repeatability. However, then the number of solved instances is
 395 lower than the actual capabilities of the hardware, the experiment takes longer, and fewer
 396 instances are solved. If we balance towards Objective (iia) obtaining maximum speed of
 397 the individual solvers, we ignore thermal management, run at maximum speed, and execute
 398 all runs sequentially. However, then throughput is low, only a low number of instances are
 399 solved, and vasts of resources on typical server CPUs are wasted. If we balance towards
 400 Objective (iib) obtaining maximum throughput during the experiment, we run a number of
 401 solvers in parallel for which there is low effect on the turbo frequency. We can obtain the
 402 value by the tool `turbostat`. For example, a turbo frequency of 3.9GHz might be acceptable
 403 over 4.7GHz if 4 additional solvers can be run in parallel. In fact, one could also simply
 404 try to repeat the experiments often to avoid balancing between Objective (iia) and (iib),
 405 which would however often require plenty of resources. If we are in Situation (i) with no
 406 access to modify the CPU thermal management capabilities or we just want to keep tuning
 407 efforts low while still having a reasonable throughput at low solving time, we can just test
 408 a reasonable setup. We lookup the thermal velocity boost (TVB) temperature, e.g., [45].
 409 Then, we execute a run with parallel solvers and sample CPU temperature. After evaluating
 410 several parallel runs, we favor a configuration where the median temperature is below the
 411 TVB temperature and the maximum temperature rarely exceeds TVB temperature.

412 3.3 CPUs and Parallel Execution

413 In the 2000s, the end of Moore’s law [69] seemed near as CPU frequency improvements for
 414 silicon-based chips started to slow down [9, 78]. Parallel computation started to compensate
 415 for this trend and multi-core hardware found its way into consumer computers around
 416 2004. In 2021, parallel hardware is widespread, for example, standard desktop hardware
 417 regularly has 8 cores (Intel i9 or Apple M1) or 12 cores (AMD Ryzen) and server systems
 418 go up to 64 cores (AMD Rome) or even 128 cores (Ampere Altra) per CPU where multiple
 419 sockets are possible. Still, parallel solving is rare in combinatorial communities such as SAT
 420 solving [35, 62] or beyond [23]. So a common question that arises in empirical problem
 421 solving is whether one can execute sequential solvers meaningful in parallel and speed-up the
 422 solution of the overall set of considered instances for an empirical experiment. While it clearly
 423 makes sense to carry out an experiment in parallel, one needs some background understanding
 424 on the hardware architecture of multi-core systems and on how to gather information about
 425 the actual system on which experiments are run. Modern systems with multiple processors on
 426 multiple sockets and processors that have multiple cores use a special memory design, namely
 427 *Non-uniform memory access (NUMA)*. There, access time to RAM depends on the memory
 428 location relative to the physical core. Each processor is directly connect to separate memory;
 429 access to “remote” RAM is still possible, but the requests are much slower since they pass
 430 through the CPU that controls the local RAM. If the operating system supports NUMA and
 431 the user is aware of the NUMA layout of the used system, the hardware architecture can
 432 help to eliminate performance degeneration that can occur due to allocation of RAM that is
 433 associated with another socket [37, 57]. The effect can be measurable, if consecutive pages

434 are used by exactly one process as done in combinatorial solving. NUMA hardware layout
435 also effects the cache hierarchy (L1, L2, often L3) and address translation buffers (TLB).
436 Recall that caches can have a measurable effect on effectiveness of combinatorial solvers [24].

437 Evidently, if running an experiment a modern operating system does not solely execute the
438 program under test. It runs function of the operating system itself, events from the hardware
439 such as input from disk, network, user-interfaces or output to graphics devices. Further,
440 programs or functions to control or monitor the program under test are running. These
441 functions might interrupt the execution of the program under test and are often triggered by
442 a mechanism called interrupt. In system programming an interrupt service routine (ISR)
443 handles a specific interrupt condition and is often associated with system drivers or system
444 calls. A common urban legend among students in the combinatorial solving community
445 is that interrupt handling happens on CPU Core 0 (monarch core) and hence no solver
446 should be scheduled on Core 0. However, this is only true when booting the system when
447 firmware hands over control to the operating system kernel. Then, only one core is running,
448 which usually is Core 0, takes on all ISR handling, initializes the system and starts all other
449 cores. In old operating systems load was not distributed to other cores by default and hence
450 the core that started the system would handle all ISRs. However, since version 2.4 Linux
451 supports a concept called SMP affinity, which allows to distribute interrupt handling [67].
452 The actual balancing and distribution of hardware interrupts over multiple cores is then
453 done by a system process, namely `irqbalance` [41]. Depending on the Linux distribution the
454 balancing is done one-shot at system start, during runtime, or entirely omitted. Nonetheless,
455 it might be helpful to understand the configured system behavior [76].

456 **Tooling for Information on the CPU.** Often, we need information on the CPU as
457 starting point for setting up parallel execution of an experiment. Linux reports information
458 on the CPU in the `proc` filesystem as text (`/proc/cpuinfo`) [10]. Among the information is
459 data about the CPU model, microcode, available cores, and instruction sets. The tool `lscpu`,
460 which is part of `util-linux` in most distributions, reports more details on the CPU such as
461 architecture, cache sizes, number of sockets, number of virtual or physical cores, number
462 of threads per core, details on NUMA regions, and active flags. More detailed information
463 on NUMA regions can be obtained by running the tool `numactl` with flag `-hardware`, using
464 `lscpu`, or by manually listing details in the `cpulist`. Note that NUMA regions and core
465 numbering can be a bit tricky as cores and NUMA regions are often not in consecutive order.

466 **Restricting NUMA, CPU, and IRQ affinity.** When running a program on a
467 multicore system, the scheduler in the operating system decides on which core the program
468 runs. In principle, this depends on the current load and on a memory placement policy
469 of the system. Some enterprise distributions have automated processes running (`numad`),
470 which automatically estimate or balance NUMA affinity. Primary benefits are reported for
471 long-running processes with high resource load, but degeneration for continuous unpredictable
472 memory access patterns. The core and allowed memory regions can also be manually restricted.
473 The tool `numactl` provides functionalities to force the execution of a program to certain
474 NUMA nodes or cores, including strict settings [51]. The tool `runsolver`, which we already
475 mentioned above, allows for setting the NUMA and CPU affinity. On modern distributions,
476 these settings can also be set when running a program by `systemd`. Literature on manually
477 tuning NUMA regions and CPU affinity reports both positive and negative effects, but less
478 than 5% performance gain on full core CPU loads [38, 43]. Hence, detailed manual tuning
479 might have a far less effect than what is usually anticipated within the community. Since
480 combinatorial solvers often rely on fast access to caches, it might be more important to
481 ensure that caches are accidentally shared between several running solvers. In principle,

p	$t_r[h]$	$f_o[\text{GHz}]$	f_{std}	$\theta_o[^\circ\text{C}]$	θ_{max}	s(1)	s(5)	s(10)	s(15)	s(25)	$t_s[h]$	s5k
1	7.37	3.90	0.26	53.4	64.0	132	179	190	191	193	3.82	161
2	4.06	3.69	0.29	60.8	72.5	125	179	189	191	193	4.27	158
4	2.49	3.30	0.28	74.2	92.0	120	175	183	190	192	5.01	150
6	1.85	2.95	0.30	76.6	94.5	111	171	181	189	191	6.03	142
8	1.77	2.81	0.46	74.5	94.0	98	160	176	183	190	6.05	131
10	1.77	2.71	0.57	74.0	92.0	88	155	174	181	189	6.78	123
12	1.59	2.59	0.51	87.0	72.5	80	147	170	176	187	10.82	117
14	1.47	2.51	0.28	91.5	72.5	88	155	174	181	189	11.17	111

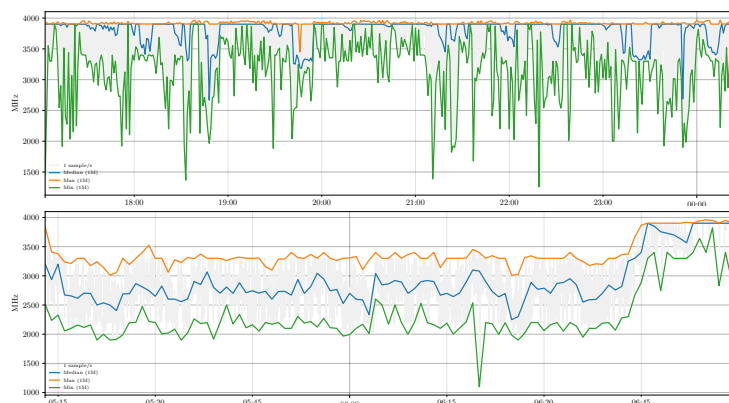
■ **Table 3** Overview on frequency scaling, thermal observations, and the number of solved instances (out of 200) on an Intel COMET LAKE (17 GEN10) processor for different number of parallel runs of the solver `CaDiCal`. The column “ p ” refers to an upper bound on the number of instances that are solved in parallel and “ $t_r[h]$ ” refers to the total runtime of the experiment in hours. While the maximum CPU frequency is 4.7 GHz, the column “ f_o ” states the observed frequency in GHz and f_{std} to its standard deviation. Column “ θ_o ” lists the observed CPU temperature; θ_{max} to the maximum temperature in $^\circ\text{C}$. The column “ $s(x)$ ” contains the number of solved instances when the runtime is cut off after x minutes. The column “ t_s ” refers to the total runtime (real-time) of the solved instances in hours at maximum runtime of 1500s for each instance. Finally, “s5k” how many instances can be solved in 5000s if instances are ordered by hardness and each run has at most 1500s. We used a simple python wrapper to start the parallel runs.

482 the IRQ affinity can be managed manually by setting dedicated flags for the system service
483 `irqbalance`. However, time might be better spent on avoiding over-committing CPUs.

484 **Suggested Tooling and Setup.** Experiments that involve measuring runtime need
485 exclusive access to the machine on which experiments are run, i.e., no other software interferes
486 in the background (e.g., running a system update, database, file server, browser, GUI with
487 visual effects) and no other users access the system in the meantime. If the hardware is used
488 for other purposes, runtime differences of 30% and more are common. If an experiment runs
489 on an HPC environment, a uniform configuration is indispensable, i.e., all nodes have the
490 same CPU, microcode, and memory layout. The number of scheduled solver resources should
491 never equal the number of cores on the system, since almost all combinatorial solvers use
492 CPU(s) at full load and operating system and measurement tools require a certain overhead.
493 If NUMA layout details are missing, one can take a rough estimate. Assume that controlling
494 and monitoring software as well as the operating system need one core per tested program,
495 add the expected number of occupied cores of the tested solver, and for a safe buffer multiply
496 the result by two. However, a better approach is to gather detailed information and test
497 whether an anticipated setup is stable. Information on the available CPUs and NUMA
498 regions can be obtained by using the tools `lscpu` and `numactl`. Modern operating systems
499 implement NUMA scheduling already well. However, it is still important to report details of
500 the system within logs of the experiments. If manual NUMA region enforcement is needed,
501 each running solver should only access the NUMA region on which it is pinned to [77]. Solvers
502 requiring fast caches should not be scheduled in parallel on cores sharing L1 and L2 cache.

503 Effects of Parallel Runs, CPU Scaling, and Timeouts in Practice

504 In the previous section, we listed complications that may occur from technical specifications
505 of modern processors and techniques present in modern operating systems. Next, we present
506 a detailed experiment on parallel execution of solvers incorporating effects of actual processor
507 frequency, stability of parallel runs, thermal issues, in combination with runtime and number



■ **Figure 1** Illustration of the CPU frequency scaling when running the sequential solver `CaDiCa1` on the considered instance set by solving in parallel 1 instance (upper) and 8 instances (lower).

508 of solved instances. We specify the setup, used measures, and common expectations of which
 509 some might be contradictory. In order to obtain a better view on effects of timeouts, we
 510 increase the maximum runtime per instance to 1500 seconds.

511 ► **Experiment 1 (Parallel Runs).** *We investigate complications of solving multiple instances*
 512 *in parallel with one sequential SAT solver on a fixed hardware.*

513 ■ *Setup: solve 200 instances by one SAT solver (`CaDiCa1`) on COMET LAKE (17 GEN10),*
 514 *maximum runtime per instance (timeout) 1500 seconds.*

515 ■ *Measures: Runtime (real-time) [h], number of solved instances, temperature (median*
 516 *of sampling each 1s the average temperature over all cores) [$^{\circ}$ C], and CPU*
 517 *frequency (median of sampling each 1s the average over all cores) [GHz].*

518 ■ *Expectation 1a: Solving should never be executed in parallel on one machine as the*
 519 *runtime and number of solved instances significantly differ otherwise.*

520 ■ *Expectation 1b: Full parallel capabilities should be employed as long as runtime and*
 521 *number of solved instances remains similar.*

522 ■ *Expectation 2: Relying on multithreading degrades runtime.*

523 ■ *Expectation 3: Measures are stable over small runtime changes.*

524 **Observations:** Results of the first experiment are illustrated in Table 3. The number of
 525 solved instances for 1, 5, 10, 15, and 25 minutes provide an overview on how many instances
 526 can be solved quickly. Unsurprisingly, the total runtime of an experiment depends on the
 527 number of parallel processes running. More precisely, the total runtime of the experiment
 528 varies between 7.37 hours and 1.77 hours when running 1 or 10 instances in parallel. Just
 529 by running 4 instances in parallel instead of 1 we cut runtime down to 33% of the original
 530 runtime and still to 55% for 2 instances. However, the total real-time of the solved instances
 531 varies between 3.82 hours and 6.78 hours (44%). The number of solved instances varies by
 532 2% at 25 minutes and 5% at 15 minutes, 13% at 5 minutes, and 33% at 1 minute timeout.
 533 When comparing the effect on the measure how many instances can be solved within 5000s,
 534 we obtain a notable 24% decrease. Surprisingly, the median CPU frequency never reached
 535 4.7GHz even when running only one instance. The actual frequency reduced significantly
 536 when more instances are running. Figure 1 illustrates the changes of the CPU frequency over
 537 time for 1 and 8 instances solved in parallel. We see that the frequency is hardly consistent
 538 and increases significantly as soon as most instances are finished and less processes run in
 539 parallel. When using multiple cores, the median CPU temperature increases significantly and
 540 may even spike (94° C) close to the maximum operating temperature of the CPU (100° C).

541 **Interpretation.** On the considered set of instances, the number of solved instances and
542 real-time over all solved instances decreases with an increasing number of instances run in
543 parallel. The effect is particularly high, if the timeout was set very low or if the measure is
544 number of instances solved within 5000s. This is not entirely surprising, since instances in
545 the considered set were selected by Hoos et al. [40] using a distribution of instance hardness
546 leading to many instances of medium hardness and a few easy and hard instances. Then, if
547 the considered timeout is low, a small constant improvement by hardware effects can increase
548 the number of solved instances notably. In contrast, there is only a 2% difference between
549 number of solved instances when timeouts are higher. The measure of solved instances within
550 5000s is particularly runtime dependent and hence configuration of the experimental setup
551 has notable effects. Regarding runtime, we can see that the real-time over all solved instances
552 almost doubles when running almost as many instances as cores are available. However,
553 the entire experiment finishes significantly faster, i.e., about 24% of the original runtime.
554 Surprisingly, the CPU frequency was far below the potential 4.7GHz. If we check more
555 details on the specification of the COMET LAKE (I7 GEN10) CPU or by running the tool
556 `turbostat`, we observe that the maximum frequency of the CPU is only 3.9GHz if 6 cores
557 are active, i.e., not explicitly suspended. While our considered system has 12 MT cores, it
558 has only 6 physical cores. Hence, we observe a measurable degeneration in number of solved
559 instances when running more instances in parallel than present physical cores are present.
560 When considering runtime, we observe a considerable increase when more than 2 instances
561 run in parallel, as CPU frequency measurably drops and temperature increases significantly.

562 **Outcome:** After summarizing observations and interpretation of our experiment, we
563 briefly evaluate phrased expectations from above. In theory, we would expect that Expec-
564 tation 1a is true for real-time and number of solved instances within 5000s, which is also
565 quite sensitive for runtime influences. Indeed, there is a measurable influence in runtime,
566 but only slightly decrease in number of solved instances, while the experiment finishes much
567 faster. If we take higher timeout, the number of parallel executions affects the runtime only
568 if already known rough estimates are exceeded. Still, the number of parallel executions is
569 influenced by throttling of the processor. Expectation 1b clearly does not hold. All measures
570 are influenced by a higher system load and hence by solving several instances in parallel.
571 While we can confirm Expectation 3 in the experiment, multithreading is not the only reason.
572 Clearly, already when using all available cores runtime and number of solved degenerate.
573 Unfortunately, our experiment does not fulfill Expectation 3. All considered measures are
574 influenced by parallel execution. Especially, limiting the total solving time is prone to
575 hardware effects and might accidentally over-highlight constant runtime improvements. Since
576 the frequency is also not stable when running only one instance, fixing the frequency might
577 be a reasonable approach during experimenting. However, if the base-frequency is exceeded,
578 a stable frequency should be estimated and experimentally verified before comparing runtime
579 and number of solved instances with multiple solvers. In our case, operating the CPU at
580 fixed 3GHz showed stable frequency results when running 1–2 instances in parallel. Under
581 the light of the mentioned complications, we fear that a single measure incorporating runtime,
582 number of solved instances, and a cutoff time is problematic if setup is neglected.

583 3.4 Input/Output

584 Input and output performance, *I/O* for short, talks about read or write operations involving
585 a storage device. On a desktop computer storage is usually restricted to local disks. On
586 cluster environments, nodes have access to a central storage over network, fast temporary
587 storage (over network), and local disks. Here, a variety of different topics are involved, for

588 example, hardware (storage arrays/network), network protocols, and file systems, which can
589 make it inherently complicated. Therefore, we provide only a brief and simple suggestion:
590 keep external influence as low as possible. When reading input and writing output, use a
591 shared memory file system (shm) to avoid external overhead. Before starting the solver under
592 test, input files are copied in-memory. Then, measuring runtime starts when executing the
593 solver, which takes as input the temporary files on the memory and outputs only to a shared
594 memory file system. The measurement ends when the solver is terminated and afterwards
595 temporary files are copied to the permanent storage and deleted from the temporary storage.
596 This approach minimizes side effects from slow network devices and avoids side effects that
597 may occur with large files and system file caches, especially when running multiple solvers
598 on the same input. However, if files are too large or solvers need the entire RAM, temporary
599 in-memory cannot be used and fast local disks (e.g., NVMe) can provide an alternative.

600 **4 Conclusion**

601 Empirical evaluations are essential to confirm observations in algorithmics and combinatorics
602 beyond theory. Many evaluations typically focus on comparing runtimes and number of
603 solved instances, since both measures are easy targets for comparison and probably roughly
604 reflect needs of end users. However, the number of solved instances is sensitive to the chosen
605 benchmark, so one has to be cautious about it. Playing devils advocate, we can even ask to
606 what extent runtime is even a meaningful measure on modern hardware. If one solver is a
607 factor of ten faster than another, we are fairly confident in it, but does modern hardware
608 allow for accurate comparisons at a range of, say, 10%, which might be the contribution of
609 an individual feature or optimization towards the hardware? Similar to experimental physics,
610 we can simply repeat an experiment often or repeat in different environments. However,
611 in combinatorial solving this is not always possible if many solvers need to be tested or a
612 reasonably high number of hard instances have to be considered. Hence, we believe that an
613 experimental setup should still be carried out thoroughly. Future work could consider up to
614 what extent certain aspects can be neglected and how repetition can circumvent minor issues.
615 In fact, our work only explains and illustrates certain complications from modern hardware
616 to make researchers aware of potential issues. In a way, we also show that complications do
617 not just concern CPU frequency, but also the experimental setup (timeouts, cutoffs, parallel
618 running processes). Clearly, there is no reason to forbid the use of certain platforms, if we
619 are aware of complications. On the meta level, we believe that clearly marking strengths and
620 weaknesses of solvers provides more insights than finding scenarios where one solver is best.

621 An interesting question for future research is the boarder topic of SIMD and branch
622 prediction, which could affect repeatability, replicability, and reproducibility. Both features
623 are quite relevant for how a good solver author can write code, but it is unclear whether
624 they can even change the overall results when comparing two solvers. In practice, one could
625 maybe investigate issues by taking different versions of a CPU (or different firmware).

626 Further, we think that papers presenting experimental evaluations could provide a simple
627 benchmark protocol as appendix, similar to literature as part of reproducibility work. Best
628 practices and checklists could be developed in a community effort after thorough discussions
629 and more detailed works. This can also include detailed guides or suggested configurations for
630 standard cluster schedulers such as Slurm [99]. Having a list of common parameters to report
631 or even practical tools could prevent manual repetitive labor. Thereby, we leave room for
632 actual scientific questions, e.g., why implementations are efficient for certain domains [91, 29].

633 Finally, our experiments focused on consumer hardware, detailed investigations with
634 server hardware are interesting for future investigations to confine limits of parallel execution.

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